Self-doping induced orbital-selective Mott transition in Hg$_2$Ru$_2$O$_7$

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Pyrochlore oxides are fascinating systems where strong multiorbital correlations in concert with geometrical frustration give rise to unanticipated physical properties. The detailed mechanism of the insulator-metal transitions (IMTs) underpinning these phenomena is, however, ill understood in general. Motivated thereby, we study the IMT in the pyrochlore Hg$_2$Ru$_2$O$_7$ using local-density approximation plus dynamical mean-field theory. In contrast to the well-known examples of Mott transitions in transition metal oxide, we show that in the negative charge-transfer situation characteristic of Hg$_2$Ru$_2$O$_7$, self-doping plays a crucial role in the emergence of an orbital-selective IMT. We argue that this mechanism has broader relevance to other correlated pyrochlore oxides.

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I. INTRODUCTION

The Mott-Hubbard insulator-metal transition (IMT) is by now recognized to play a central role in our understanding of d- and f-band compounds. Understanding the complex interplay between strong multiorbital (MO) electronic correlations, structural distortions, and strongly anisotropic orbital-dependent hopping holds the key to a consistent theoretical description of their unique responses. Adding geometric frustration to the above results in a truly formidable problem. In geometrically frustrated systems, the exponentially large degeneracy of classical ordered states inhibits emergence of conventional order, permitting new, complex ordered ground states to arise. In real systems, structural effects may partially remove this huge degeneracy, making the problem (counterintuitively) somewhat simpler to solve. However, in near-undistorted cases, near-perfect orbital degeneracy, and the consequent strong quantum orbital and spin fluctuations in a highly degenerate system underpin their physical behavior.

The recently discovered pyrochlore system, Hg$_2$Ru$_2$O$_7$, is a particularly interesting case in this context. As temperature $T$ is reduced, the anomalous (see below) non-Fermi-liquid (nFL) metallic state becomes unstable, via a first-order Mott transition, to an antiferromagnetic (AF) Mott-Hubbard insulator (AFI). External pressure ($p$) melts the AFI beyond a critical $p_c=6.0$ GPa, resulting in a low-$T$ correlated FL behavior for $T<T^*=13$ K. At ambient pressure, the IMT transition is accompanied by lowering of lattice symmetry from (high-$T$) cubic to a (low-$T$) lower, hitherto precisely unknown, type: depending upon its precise type, either AF or dimer order may be possible.

The high-$T>T^*$ state in Hg$_2$Ru$_2$O$_7$ is an anomalous nFL: the dc resistivity $\rho(T)=T$ for $T>T_{\text{MI}}=108$ K (Ref. 4) at ambient pressure, and deviates from the FL form for $T>T^*$ beyond $p_c$. The uniform spin susceptibility is Curie-Weiss type for $T>T_{\text{MI}}$ indicating a strong local-moment scattering regime. The nFL character is also borne out from the recent photoemission (PES) data, showing anomalously broad PES line shapes, with no hint of Fermi-liquid (FL) quasiparticles, in the metallic phase. Given the cubic pyrochlore structure for $T>T_{\text{MI}}$, strong orbital (from $t_{2g}$ orbital degeneracy) and spin fluctuations are implied. How might strong scattering processes involving these fluctuations produce the observed nFL metal? What drives the AFI as $T$ is lowered? A correlated electronic structure study which can illuminate these issues does not, to our best knowledge, exist. In this work we study precisely these issues in part in Hg$_2$Ru$_2$O$_7$ using the local-density approximation plus dynamical mean-field theory (LDA+DMFT) method. We focus on the mechanism of the $T$-driven IM transition, and leave the issue of the low-dimensional AF with a spin gap for future consideration.

II. MODEL AND SOLUTION

Starting with the high-$T$ cubic $F\bar{4}3m$ structure found by Klein et al., LDA band-structure calculations were performed using a (scalar and fully relativistic) full-potential local-orbital (FPLO) scheme and a linear muffin-tin orbital (LMTO) scheme in the atomic sphere approximation. In Fig. 1 we display our FPLO-LDA (Ref. 11) results for the one-particle density of states (DOS). Clearly, the major contribution to the DOS comes from Ru 4$d$ and O(1) 2p orbitals, but the O(2) 2$p$ orbitals also have noticeable spectral weight at the Fermi level ($E_F$). As seen in Fig. 1, the influence of the spin-orbit coupling in the cubic phase to the $t_{2g}$ states near $E_F$ is negligible. Further, we observe strong hybridization between Ru 4$d$-O(1) 2$p$ orbitals, and between O(2) 2$p$-Hg 6$s$ orbitals, but weak mixing between these two sets. These important findings will be exploited below to study the physics of Hg$_2$Ru$_2$O$_7$ using a multiorbital Hubbard model involving only the $d$-band sector. At one-particle level, the corresponding model Hamiltonian reads $H_{\text{band}}=\sum_{k,a}e_{k,a}d_{k,a}^\dagger d_{k,a}+\sum_{\ell,\alpha=\pm 1}\Delta_{\ell} (n_{\ell a}^\dagger n_{\ell a}^\dagger)-\Delta_{\ell} (n_{\ell a}^\dagger n_{\ell a}^\dagger)$ (Ref. 12) the $t_{2g}$ orbitals, $\Delta_{\ell}$ ($\ell=1,2$) are the $pd$ charge-transfer (CT) terms involving two Ru-O(1) ($\ell=1$) and Ru-O(2) ($\ell=2$) channels. Clearly, neither an AFI nor a nFL metal can be expected at this level, this requiring a reliable treatment of strong $d$-shell electronic correlations. This part reads
Hg₂Ru₂O₇. Of course, this is an approximation. It is, how-
the negative charge-transfer situation that is obtained in
function is to simulate the self-doping process arising from
channel by replacing the latter by a "reservoir," whose only
stance. This can occur via a
processes involving the O 2p
states. Because of the negligible one-particle mixing
understood as a band of hybridized O 2p
higher energies.

$$H_{\text{int}} = U \sum_{i,a} n_{d,i}^{a} n_{d,i}^{a'} + U' \sum_{i,a,a'} n_{d,i}^{a} n_{d,i}^{a'} - J_H \sum_{i,a,a'} S_{i,a} \cdot S_{i,a'},$$

(1)

with $a,a' = e_{g1}, e_{g2}, a_{1g}$. Given the larger spatial extent of 4d orbital vis-à-vis their 3d counterpart, we also include a
Madelung term, $H_M = U_{pd} \sum_{(i,j),a} n_{d,i}^{a} n_{d,j}^{a}$, in our calculations
(see below). In Tl₂Mn₂O₇, the IMT [from a paramagnetic
insulator (PI) to a ferromagnetic metal (FMM)] is seemingly
驱动 by the Tl 6s states crossing $E_F$ across $T_c$, for in-
stance. This can occur via a $T$-dependent CT from the TM $d$
states to the O(2)-Tl hybridized states. In view of the generic
relevance of self-doping in TM 4d pyrochlores, this term is
an essential part. In the low-$T$ phase, this will involve CT
processes involving the O 2p-Hg 6s channel (second term of
$H_{\text{band}}$) across the IMT, as we describe below.

The $d_{a,a'}$ above should be understood as appropriate RuO₄
cell-centered combinations of the Ru 4d and O 2p orbitals,
computed within LDA. Similarly, the $b = 2$ channel is to be
understood as a band of hybridized O 2p and Hg 6s orbital
states. Because of the negligible one-particle mixing (hybrid-
ization) between the $b = 1,2$ channels, we approximate the
full problem of three Ru $d$ bands coupled to the $b = 2$ band channel by replacing the latter by a “reservoir,” whose only
function is to simulate the self-doping process arising from
the negative charge-transfer situation that is obtained in
Hg₂Ru₂O₇. Of course, this is an approximation. It is, how-
ever, a good one: the $b = 2$ band channel has appreciably
smaller DOS around $E_F$ in the LDA results. In a DMFT-like
approximation, with negligible one-particle hybridization be-
 tween the $b = 1,2$ bands, the inter-site Madelung term will
push this small spectral weight away from $E_F$, to lower and
higher energies. (Notice that the O 2p bands will be split by
$U_{pd}(n_{d,z})$, where $z$ is the coordination number of the lattice,
and hence quite large.) This will already occur at the level of
LDA+Hartree approximation. We then expect that the cor-
related spectral function will be dominated by the $d$ bands
over an appreciable range about $E_F$. Correlation effects in
Hg₂Ru₂O₇ via LDA+DMFT are studied below, subject to
this caveat. We will show that this is indeed a good approxima-
tion a posteriori, in the sense that our LDA+DMFT re-
results with the above caveat show very good quantitative
agreement with one-particle spectroscopy and key thermody-
namic and transport data in Hg₂Ru₂O₇.

The full many-body Hamiltonian reads $H = H_{\text{band}} + H_{\text{int}}$
$+ H_M$. We use this model within MO-DMFT developed and
used for a range of transition metal oxide (TMO) with good
success. We use the MO-iterated perturbation theory (IPT)
as an impurity solver in the DMFT self-consistent procedure.
Though not numerically exact [such as quantum Monte
Carlo (QMC), numerical renormalization group (NRG), and
dynamic density matrix renormalization group (D-DMRG)],
it has many advantages: it is valid for $T = 0$, where QMC
cannot be used. NRG and D-DMRG are extremely prohibi-
tive for three orbital models, even without electronic struc-
tural inputs at LDA level. As shown in earlier work, DMFT(MO-IPT) generically gives very good semiquantita-
tive agreement with PES and x-ray-absorption (XAS) experi-
ments for TMOs. For Hg₂Ru₂O₇, DMFT(MO-IPT) has to be
extended to treat the second CT channel described above.
Given the complexity of the problem, we choose the follow-
ing strategy to solve $H$ above. For the high-$T$ phase, (i) we solve $H_{\text{band}} + H_{\text{int}}$ within DMFT(MO-IPT) version used ear-
ier; for technical details see Ref. 15. (ii) As indicated by
experiment on the related Tl₁Ru₁O₃ system, we study the
effect of Ru 4d-O(2) 2p-Hg 6s CT processes by incorporat-
ing this CT channel self-consistently into the LDA+DMFT(MO-IPT)
procedure: given the small Ru 4d-O(2) 2p hybridization, the O(2) 2p-Hg 6s channel acts like a scattering (nonhybridizing) channel for the Ru $t_{2g}$
bands in the impurity model of MO-DMFT. This enables us
to treat this extra channel by combining the MO-IPT solution for
(i) with the exact DMFT solution of a Falicov-Kimball
model (FKM) for (ii), in a self-consistent way.

III. LDA+DMFT RESULTS AND DISCUSSION

We now describe our LDA+DMFT results. We start with the
(cubic) pyrochlore structure at high $T$, with the corre-
sponding LDA DOS as the input for the MO-DMFT calcula-
tion with total 4d occupation, $n_d=3$. Further, we work in
the LMTO (Ref. 18) representation in which the one-particle
density matrix is diagonal in the $t_{2g}$ orbital index, so that
$G^{(0)}_{a\bar{b}}(k,o) = \delta_{a\bar{b}} C^{(0)}_{a\bar{b}}(k,o)$. We choose $U=5.5$ eV, $J_H$
$=1.0$ eV, and $U''=(U-2J_H)=3.5$ eV for the Ru 4d shell,
along with $U_{pd}=1.5$ eV, as representative values for
Hg₂Ru₂O₇. We believe that $U, J_H$ do not vary much for 4d
TMO pyrochlores and, in fact, $U=5.0$ eV was found for the
CT insulator Cs₂AgF₄.

A. Metallic phase

In Fig. 2, we show the correlated many-particle spectral
function for the metallic phase of Hg₂Ru₂O₇. The dynamical
spectral weight transfer (SWT) over large energy scales,
characteristic of strong local correlations, is explicitly mani-
fest. More interestingly, the metal has an orbital-selective

FIG. 1. (Color online) LDA band structure for cubic Hg₂Ru₂O₇.
O(1) [O(2)] denotes oxygen ions nearest to Ru (Hg).

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(OS) character: the $a_{1g}$ DOS is almost “Mott” localized, even as the $e_g$ DOS develops a precursor of a low-energy pseudogap, characteristic of an incoherent metal behavior. This is further corroborated by examining the orbital-dependent self-energies $\Sigma(\omega)$; see inset of Fig. 2. Clearly, the $e_g$ (imaginary part of) $\Sigma(\omega)$ shows quasilinear frequency dependence near the Fermi energy $|\omega-E_F|<0.3$ eV, while $\text{Im } \Sigma_{a_{1g}}(\omega)$ shows quadratic behavior. This describes a nFL metal, with a linear-in-$T$ quasiparticle damping rate. Within DMFT, this is also the transport relaxation rate, since vertex corrections drop out in the computation of the conductivities in this limit. The dc resistivity is then given by $\rho_{dc}(T)=(m^*/ne^2)\text{Im } \Sigma_{e_g}(\omega=T)=AT$, in accord with the linear-in-$T$ resistivity observed experimentally in the “high-$T$” metallic phase. Moreover, the selective localization seen in the $a_{1g}$ orbital DOS gives rise to unquenched local moments coexisting with “itinerant” (but incoherent as derived above) $e_g'$ carriers naturally giving a Curie-Weiss form of the spin susceptibility, which is also observed right up to the IMT. We have also estimated the $\gamma$ coefficient of the metallic specific heat from the real part of $\Sigma_{g}(\omega)$ (not shown) as $\gamma/\gamma_{\text{LDA}}=4.25$: this seems to be in the range estimated in Ref. 4. Actually, the noticeable $T$ dependence of $\gamma$ above $T_{\text{MI}}$ (Ref. 4) is additional evidence of disordered local moments in the “bad” metal, and further supports our picture.

Using the LDA+DMFT result, we also compare (Fig. 3) our computed PES line shape with very recent work from the RIKEN-SPring 8 group.7 Given our restriction to the $t_{2g}$-Ru $4d$ bands in the MO-DMFT (Hg $d$ and O $2p$ bands will start contributing at higher binding energies, as seen from LDA), good quantitative agreement with experiment is evident up to $-2.0$ eV, lending strong support to our theoretical work. Additionally, we predict that an intense peak will be seen around $0.4-0.5$ eV in x-ray absorption studies, as in $\text{Tl}_3\text{Ru}_2\text{O}_7$.21

In fact, the LDA+DMFT spectral functions show that at low energy the full MO problem is mapped onto an effective FKM-like model.15 since the bad metal is of the orbital-selective type. There, the problem in the local limit corresponds to itinerant (but incoherent) $e_g'$ carriers scattering off (Mott) localized $a_{1g}$ electronic states. The resulting problem is precisely the “x-ray-edge” problem in DMFT.25 We now understand the structure of the self-energies, and the nFL behavior, as an interesting manifestation of the Anderson orthogonality catastrophe (OC) caused by this x-ray-edge mapping. Building upon this understanding, using DMFT, we predict for $T>T_{\text{MI}}$ the following:

(a) The optical conductivity will show a low-energy pseudogapped form, characteristic of an incoherent (nFL) metal. Polarized optical studies should indicate the OS character of the nFL state.

(b) Given the local version of the Shastry-Shraiman relation,23 the electronic Raman line shape should show a continuum response, cut off by a pseudogap feature at low energy.

**B. Insulating phase**

Now, we turn to a description of the insulating phase. A naive search for the instability of the nFL to a Mott-Hubbard insulating state, where $U,U'$ were increased to unphysical values, nevertheless turned out to be unsuccessful. This is a clear indication of involvement of additional electronic-cum-structural effects in driving the IMT. The observed structural change across $T_{\text{MI}}$ (Refs. 4 and 5) supports this reasoning. From the LDA orbital assignment, it is clear that an additional structural change necessarily involves partial occupa-
tion of the twofold-degenerate $e_g'$ orbitals. Starting from the nFL metal derived above, this can only occur via a $T$-dependent change in the "self-doping" process.\textsuperscript{14} As in Tl$_3$Ru$_2$O$_7$, this $T$ dependence could be provided by electronic coupling to the Ru-O stretching phonon mode, which is experimentally observed to split below $T_M$.\textsuperscript{14} This would imply a structural change setting in below $T_M$, whose precise nature is hitherto unknown.

Motivated by this observation, we argue that this resulting change in the Ru $4d\rightarrow O(2)\ 2p$ CT leads to a partial $4d$ occupation, induces orbital order, and lifts the $e_g'$ degeneracy via a structural distortion. Within DMFT, this will reduce the orbital-dependent hoppings, driving large SWT from low to high energy, and stabilize the second (Mott-Hubbard insulating) solution of the DMFT equations. This is indeed seen in the LDA+DMFT calculation, as we show below.

Based on this reasoning, we explore the Mott-Hubbard insulating phase of Hg$_2$Ru$_2$O$_7$, by searching numerically for the instability of the first (metallic) solution found above the second (insulating) solution of the DMFT equations in the quantum paramagnetic phase. The DMFT(MO-IPT) equations are solved with $U$, $U'$, $U_{pd}$, and $n_i=2.6$. We vary $n_i$ in trial steps, and look for a critical $n_i^{(c)}$ which stabilizes the PI solution of the DMFT equations. As discussed above, and indeed seen in the inset of Fig. 3, partial occupation of the $4d$-$e'_g$ orbitals leads to removal of the orbital degeneracy, and the corresponding modification of orbital orientation gives rise to a reduced inter-site one-electron overlap. Within MO-DMFT, this triggers the Mott-Hubbard insulating state via large SWT on a scale of 5.0 eV, as seen in Fig. 2. Hence, the IMT is an OS Mott transition. Importantly, however, notice that the self-doping process leading to fractional $d$-orbital occupation is a crucial ingredient. Thus, in contrast to other OS cases,\textsuperscript{15} the IMT in Hg$_2$Ru$_2$O$_7$ is driven by the self-doping in the negative CT situation, $\Delta_e=(\epsilon_{e_1}-\epsilon_{e_2})=(-2.8\ eV+1.3\ eV)=-1.5\ eV$. Along with the microscopic elucidation of the nFL behavior, the agreement with PES in the nFL metal phase up to $\omega=2.0\ eV$ (Fig. 3) constitutes strong evidence in favor of our mechanism for the IMT in Hg$_2$Ru$_2$O$_7$. Quantitative comparison with PES in the low-$T$ phase requires an extension of our approach to include short-ranged (intersite) orbital and spin correlations characteristic of pyrochlores. This requires a cluster-DMFT analysis, presently a forbidding prospect. Nevertheless, observation of a Curie-Weiss spin susceptibility right up to the IMT,\textsuperscript{24} along with the excellent agreement with PES in the nFL, justifies the use of DMFT to describe the IMT.

We emphasize that this is a different picture for the IMT in correlated systems. In contrast to the early TMO, which are Mott-Hubbard insulators ($U_{dd}>\Delta$ in the Zaanan-Sawatzky-Allen scheme),\textsuperscript{25} the Ru $4d$-O(1) $2p$ CT channel, along with the Madelung term, is important in Hg$_2$Ru$_2$O$_7$. In the DMFT context, the importance of the CT energy in the late-TMO is recognized.\textsuperscript{26} Our work shows the relevance of CT energy for the IMT in a MO pyrochlore system. Further, it is likely to be more broadly generic to pyrochlore TMOs. Recall that in Tl$_3$Mn$_2$O$_7$, the PI-FMM (Ref. 13) transition is driven by the shift of the Ti 6$s$ band through $E_F$ across $T_c$. This is readily rationalized in our picture, in terms of the “switching on” of the Mn $3d$-O(2) $2p$-Ti 6$s$ CT channel across $T_c$ in Tl$_2$Mn$_2$O$_7$.\textsuperscript{13}

The correlation between the CT process detailed above and the IMT is also visible in a whole family of 4$d$ pyrochlores, $A_2$Ru$_2$O$_7$, with $A=$Pb,Bi,Y.\textsuperscript{21} The low-$T$ magnetic ordering in the Mott-Hubbard insulating phase(s) may, however, be quite different, being sensitively dependent on the nature of the structural change across the IMT, as well as on spin state. For example, the spin $S=1$ system, Tl$_3$Ru$_2$O$_7$, shows a very similar Mott transition; however, the low-$T$ phase is found to be a Haldane spin chain.\textsuperscript{27} In Hg$_2$Ru$_2$O$_7$, the half-integer spin $S=3/2$ rules out the Haldane analogy. If the low-$T$ magnetic structure corresponds to having Ru chains, as in Tl$_3$Ru$_2$O$_7$, one would have an AF ground state with gapless spin excitations. Observation of the spin gap in the uniform spin susceptibility in Hg$_2$Ru$_2$O$_7$ may therefore point to the relevance of the spin-orbit coupling in the insulating phase: this will induce Ising-type anisotropy in an $S=3/2$ Heisenberg chain and generate a gap to spin excitations.$^{28}$ More experimental work is also called for to pinpoint the specific factors affecting this issue. Given the structural distortion necessarily accompanying the IMT caused by lifting of the $e_g'$ degeneracy in Hg$_2$Ru$_2$O$_7$, more detailed theoretical work awaits more precise characterization of the low-$T$ structure of Hg$_2$Ru$_2$O$_7$. We plan to address the issue of magnetic order and its associated excitation spectrum in the low-$T$ (insulating) phase of Hg$_2$Ru$_2$O$_7$ in a future work.

IV. CONCLUSION

In conclusion, we have performed LDA+DMFT calculations to demonstrate the role of multiorbital electron-electron interactions on the electronic structure of a recently discovered pyrochlore system, Hg$_2$Ru$_2$O$_7$. This system exhibits a first-order temperature-dependent IMT. The high-$T$ metallic phase is shown to be an orbital-selective non-Fermi liquid, signaled by a quasilinear frequency dependence of the imaginary part of the correlated self-energy and the absence of quasiparticle peaks in the orbital-selective spectral functions at very low frequencies. The LDA+DMFT spectral function shows good quantitative agreement with recent PES data, showing anomalously broad PES line shapes, as well as with the linear-in-$T$ resistivity and mass enhancement in the metallic phase. In stark contrast to the better-known examples\textsuperscript{1} of Mott transitions in 3$d$ transition-metal compounds, our results imply a different mechanism for MIT in the 4$d$ pyrochlore-based electron systems (such as Hg$_2$Ru$_2$O$_7$). Namely, a negative charge-transfer associated self-doping drives an orbital-selective MIT at low temperatures via the Mott-Hubbard route. Our study should be more generally applicable to MO pyrochlore systems and, in particular, to Tl$_3$Mn$_2$O$_7$, exhibiting Mott-Hubbard transitions.\textsuperscript{14,21,24,29} as functions of suitable “tuning parameters.”

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7 A. Chainani (private communication).
11 Self-consistency was obtained on a 12 × 12 × 12 k mesh for the full Brillouin zone.
12 Within the LMTO framework, the diagonalized combination of the t_{2g} orbitals reads |e_{g}^{(1)}⟩=0.195(|d_{z^2}⟩−|d_{xy}⟩)+0.888|d_{x^2−y^2}⟩, |e_{g}^{(2)}⟩=0.888|d_{z^2}⟩+0.112(2|d_{xz}⟩+|d_{yz}⟩), |a_{g}⟩=0.577(|d_{z^2}⟩+|d_{x^2−y^2}⟩).
18 Self-consistency is reached by performing calculations on a 12 × 12 × 12 k mesh for the Brillouin integration. The radii of the atomic spheres were chosen as r_{H}=2.8781 (Hg), r_{Ru}=1.8712 and 2.1247 [O(1) and O(2)], and r_{Ru}=2.4971 (Ru) (in a.u.) in order to minimize their overlap.